# A DIDACTIC INTRODUCTION TO NETWORK NEUROSCIENCE FOR COMPUTATIONAL PSYCHIATRY

#### WHERE WE ARE AND WHERE WE COULD GO

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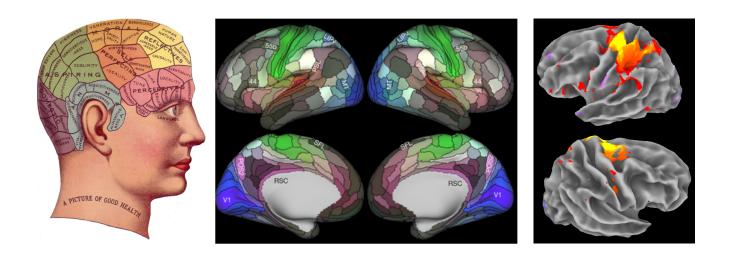
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### **Brief Outline**

- I. Introduction to and background for the computational framework
- II. Case study of one form of its application
- III. Short description of other uses
- IV. Limitations of the technique, rules of the road problems, perils
- V. Options
- VI. Summary

### I. The challenge of distilling rules & mechanisms in brain



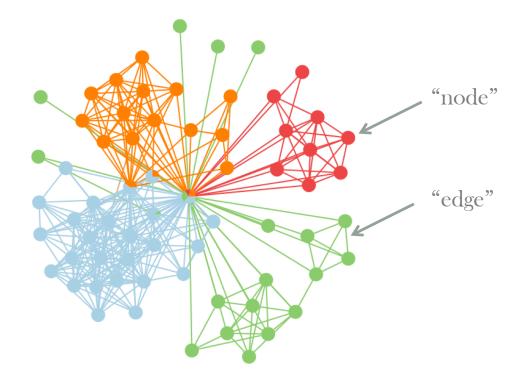
In general, psychiatric conditions are not associated with alterations in a single brain region. Instead, there is a constellation of brain regions and their (structural or functional) connections that are altered.

This complexity produces complex changes in cognition and behavior, and significantly hinders progress in understanding and in the development of effective interventions.

#### Network Science

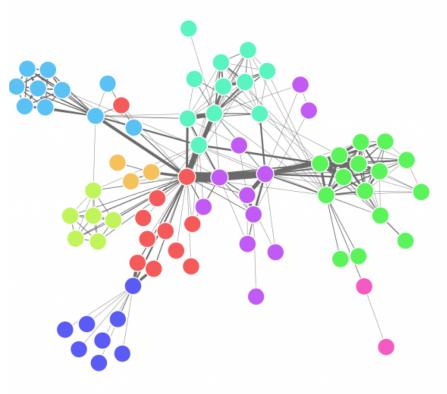
Network science is a natural language in which to frame complex constellations of regions and their connections.

Network science is an emerging academic field that studies *complex networks*, considering distinct elements represented by nodes and the connections between the elements as edges.



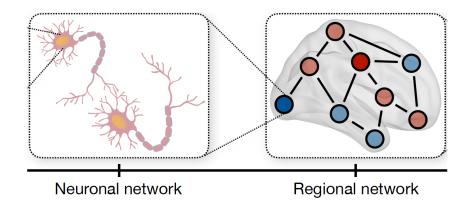
## Strengths of the network science approach

• Flexible framework that is applicable to many data types, and useful for testing scientific hypotheses in different domains.



### Multiscale, multilayer, multiplex networks

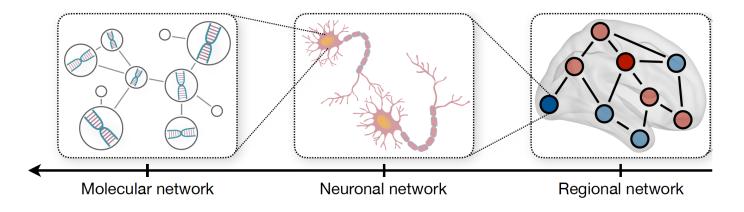
Large-scale brain activity provides a coarse-grained encoding of neural processes, and the map from cellular dynamics to regional dynamics reflects rules of system function.



How do cellular processes shape circuit behavior?

### Multiscale, multilayer, multiplex networks

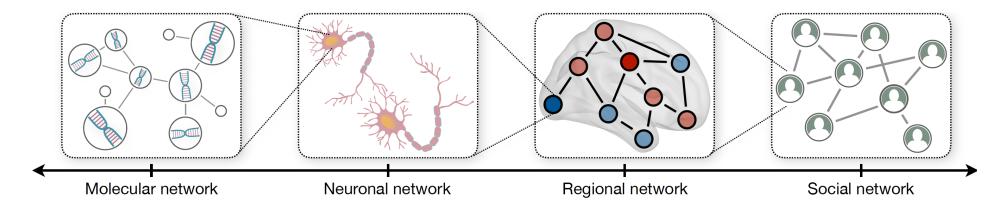
Understanding how molecular mechanisms affect large-scale brain network function is critical for the development of effective pharmacological interventions.



How do genetic material and epigenetic drivers shape circuit behavior across spatial scales?

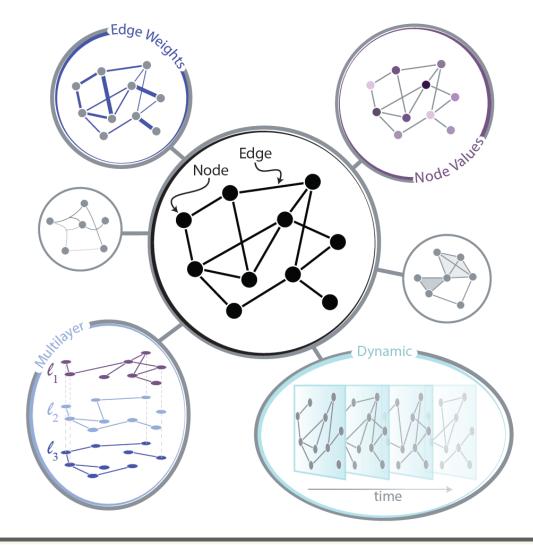
## Multiscale, multilayer, multiplex networks

While brain activity and structure offer biological mechanisms for human behaviors, social networks offer external inducers or modulators of those behaviors.



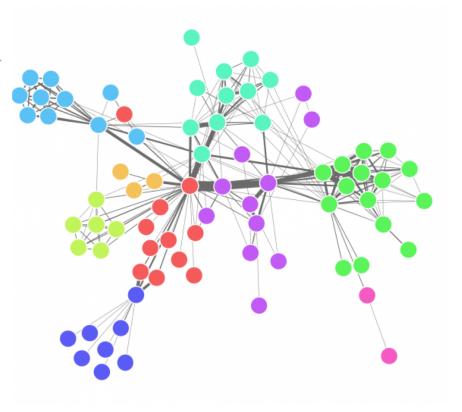
How do brains shape social networks? How do social ties shape the brain?

## Encoding different sorts of network models



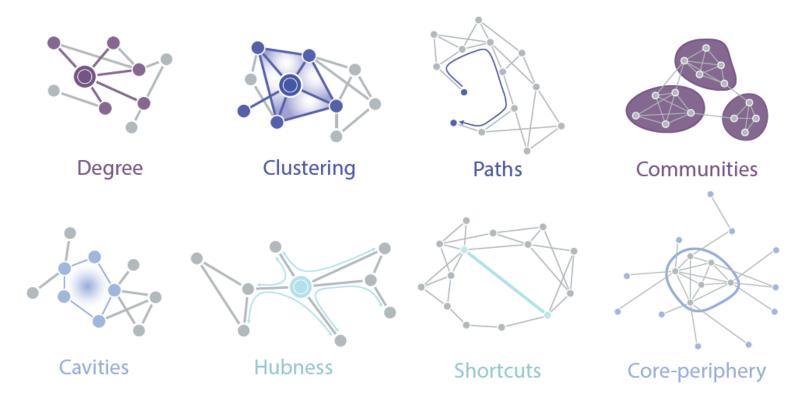
## Strengths of the network science approach

- Flexible framework that is applicable to many data types, and useful for testing scientific hypotheses in different domains.
- Provides a rich set of statistical tools, computational algorithms, and theories developed in math, physics, engineering, and computer science.



## Statistical tools to probe network architecture

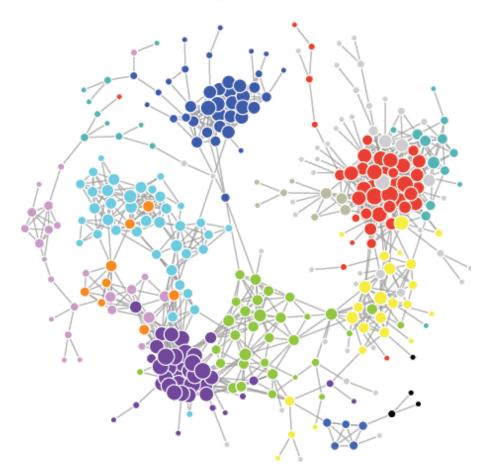
Network statistics allow us to quantitatively characterize neural circuits, behaviors, and symptoms characteristic of psychiatric disorders, and to distinguish between groups of subjects either within the disorder or between disorders.

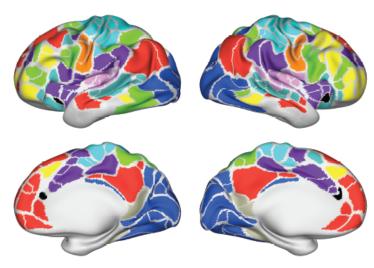


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### II. Case Study





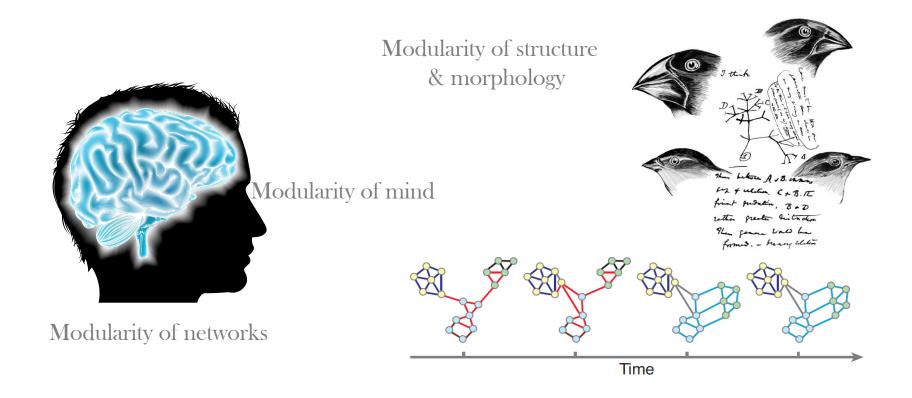
Structural or functional connections between diverse brain areas.

The latter estimated either at rest or during the performance of tasks thought to activate circuits relevant for psychiatry.

Goal: to understand the architecture of structural or functional circuitry underlying cognitive deficits in disorders of mental health.

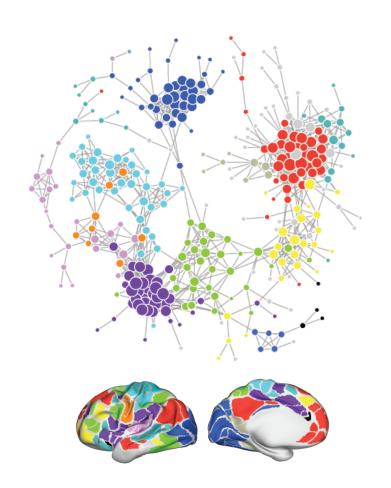


### Network substrates for adaptation & learning



Are brain networks modular? Does modularity help us to understand large-scale neural signatures of adaptation and learning?

### Theoretical & Computational Challenges



Challenge: Parsimoniously representing and describing complex connectivity patterns.

- > Network models
- Bassett, Zurn, Gold (2018) Nat Rev Neuro

Challenge: Detecting modular structure in network models of brain connectivity.

- ➤ Modularity maximization (NP Hard)
- Meunier et al. (2009) NeuroImage

$$Q = \sum_{ij} [A_{ij} - P_{ij}] \delta(\sigma_i \sigma_j)$$

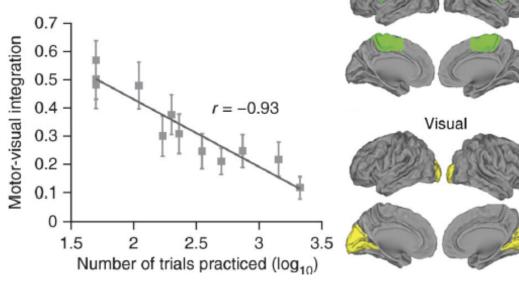
Challenge: Detecting evolving modules.

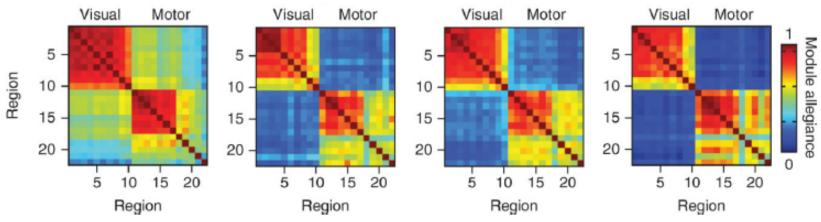
- ➤ Multilayer modularity maximization
- Mucha et al. (2010) Science

$$Q_{multi} = \frac{1}{2\mu} \sum_{ijls} [(\mathcal{A}_{ijl} - \gamma_l \mathcal{P}_{ijl}) \delta_{lm} + \omega_{jlm} \delta_{ij}] \delta(c_{il}, c_{jm})$$

## Module Autonomy in Sequence Learning

The coherence between motor and visual modules decreased markedly with training, suggesting a growing autonomy.

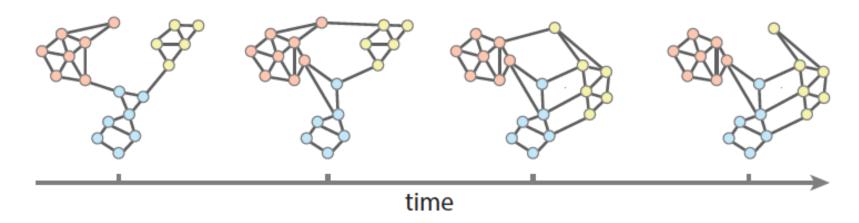






Motor

### Flexible modularity supports executive functioning



Flexibility in network modules is predicts individual differences in:

Visuo-motor learning (Bassett et al. 2011 PNAS)

Future learning (Mattar et al. 2018 NeuroImage)

Learning rate (Gerraty et al., 2018, *J Neurosci*)

Cognitive flexibility (Braun et al. 2015 *PNAS*)

Working memory (Braun et al. 2015 PNAS)

(Shine et al. 2016 Neuron)

Planning & reasoning (Pedersen et al. 2018 PNAS)

Intermediate Phenotype for Schizophrenia

(Braun et al. 2016, *PNAS*)

Medication (Braun et al. 2016, PNAS)

Mood (Betzel et al. 2017 Sci Rep)

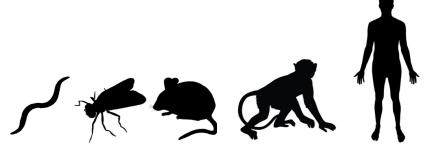
Intervention-related plasticity (Gallen & D'Esposito 2019 TICS)



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#### III. Other Uses



1. Neural systems & genetics across species & scales

Betzel & Bassett Multiscale brain networks (2017) NeuroImage Van den Heuvel et al. Comparative connectomics (2016) TICS Fornito et al. Connectome & transcriptome (2019) TICS

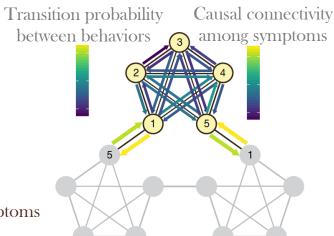
2. Behavior

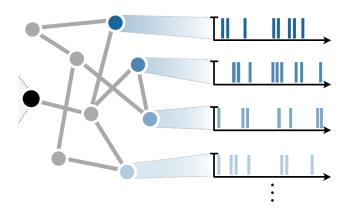
Kahn et al. Network constraints on learnability .... (2018) *Nature Human Behavior* Stereotypies, risk-taking, substance use, ...

3. Symptoms

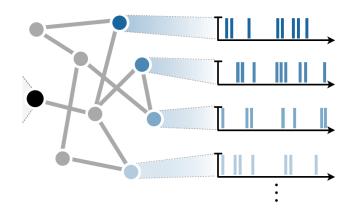
Yang et al. Socioemotional dynamics ... of depressive symptoms (2018) *Complexity* 

Anger, anxiety, depressed mood, difficulty concentrating, sleep problems, restlessness ...



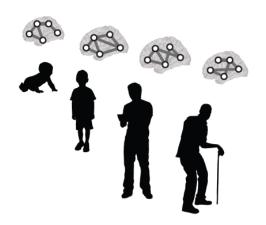


Denk et al. 2012 Nature Reviews Neuroscience

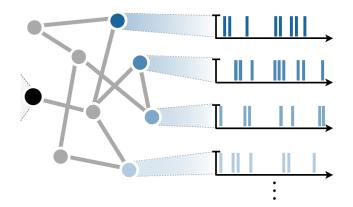


Denk et al. 2012 Nature Reviews Neuroscience

### Network Development

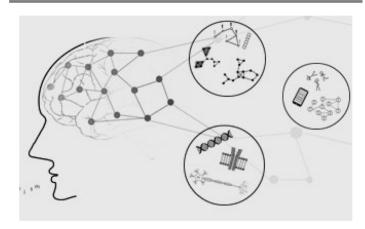


Di Martino et al. 2014 Neuron



Denk et al. 2012 Nature Reviews Neuroscience

### Network Pathology

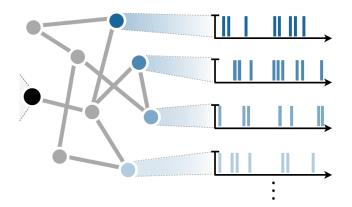


Stam 2014 Nature Reviews Neuroscience Braun et al. 2018 Neuron

#### Network Development

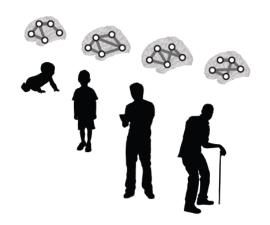


Di Martino et al. 2014 Neuron



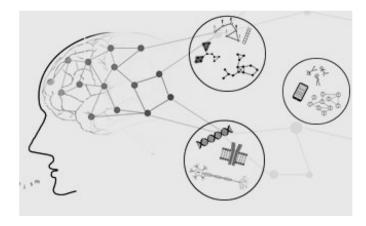
Denk et al. 2012 Nature Reviews Neuroscience

#### Network Development



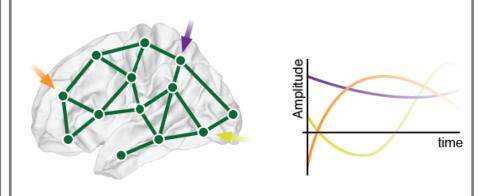
Di Martino et al. 2014 Neuron

### Network Pathology



Stam 2014 Nature Reviews Neuroscience Braun et al. 2018 Neuron

#### **Network Intervention**



Tang et al. 2018 Review of Modern Physics

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### IV. Models make assumptions



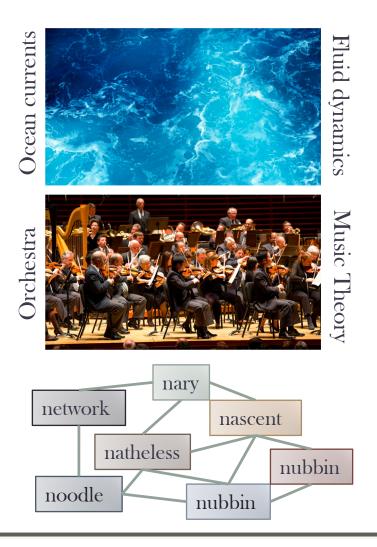
Network science is a modeling assumptions.

Assumption 1: You can separate the system into cleanly delineated units.

Assumption 2: You can define the most salient relations or connections between units.

Assumption 3: From the structure of the connectivity pattern, one can learn about a system's organization, make educated guesses about its function, and build models of its development, growth, or evolution

### Example violations of assumptions

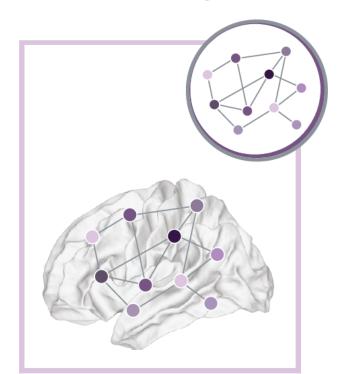


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### Evaluating and testing the validity of network models



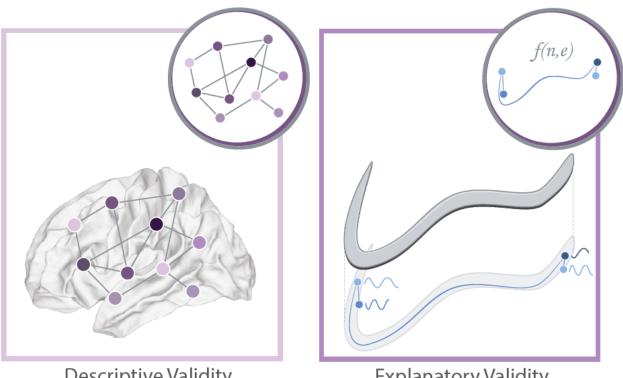
**Descriptive Validity** 

The validity of a particular network model depends on the goals of its use and the domains of its application.

Descriptive validity addresses the question of whether the model resembles in some key way(s) the system it is constructed to model. It aligns with questions about how well the specific patterns of nodes and edges matches the anatomical and/or functional data that it represents.



### Validity of network models



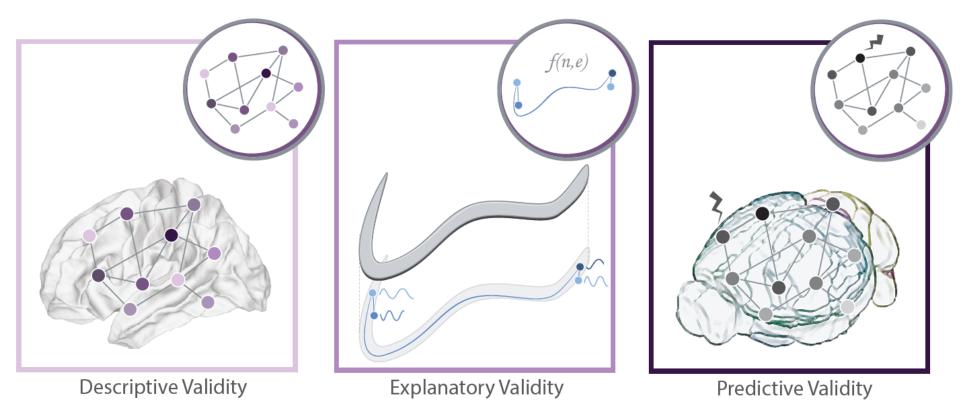
**Descriptive Validity** 

**Explanatory Validity** 

Explanatory validity focuses on a theoretical construct used to develop statistical tests and support conclusions drawn from the use of the model. It addresses whether a network's architecture can be justified from data and used to test for causal relations to dynamics or behavior based on that architecture.



### Validity of network models



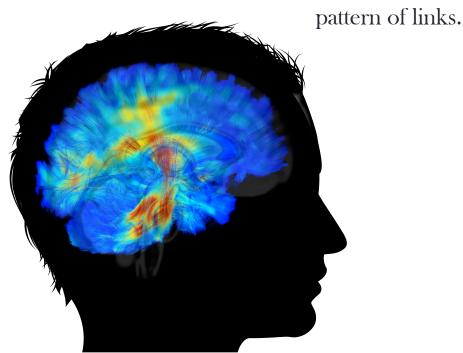
Predictive validity occurs when there is an organism-model correlation in response to a perturbation, such as a drug, electrical or chemical stimulation, neurofeedback, or training.

### **Brief Outline**

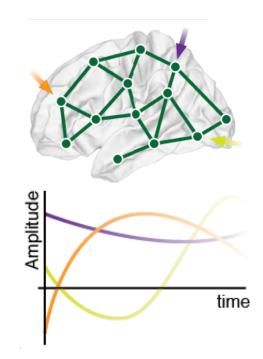
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## V. Options: Moving closer to predictive validity

First note that the propagation of signals in a networked system depends on the



What we have: A network of structural links empirically measured by neuroimaging.

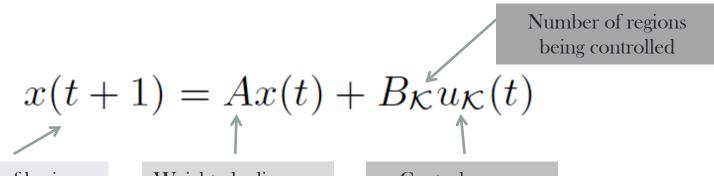


What we seek: A theory for how a change in activity in one region affects activity in other regions.



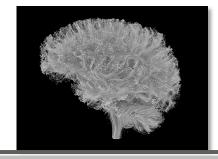
### Formalizing the Problem of Network Control

- Neural processes can be approximated by linearized generalizations of nonlinear models of cortical circuit activity (Galan 2008; Honey et al. 2009).
- We consider a noise-free linear discrete-time and time-invariant network model:



State of brain regions over time

Weighted adjacency matrix Control energy





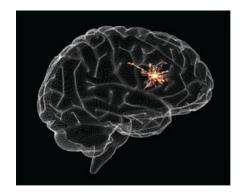
### Is the brain theoretically controllable?

How controllable the network is can be estimated using the smallest eigenvalues of the T-steps controllability Gramian:

$$W_{\mathcal{K},T} = \sum_{\tau=0}^{T-1} A^{\tau} B_{\mathcal{K}} B_{\mathcal{K}}^{\mathsf{T}} (A^{\mathsf{T}})^{\tau}$$

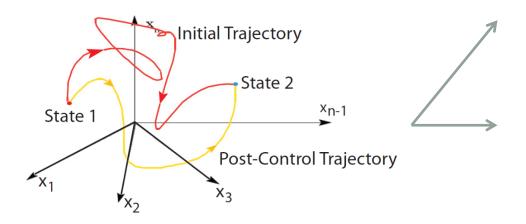
For brain networks, this value was small:  $2.5 \times 10^{(-23)}$ 

Practically extremely hard to control



### Types of driver nodes

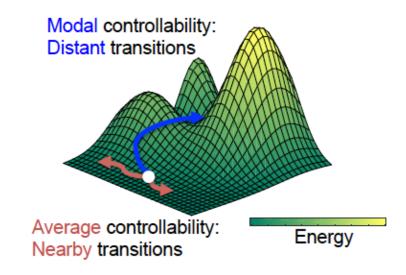
➤ Which regions of the brain are most efficient or most difficult to control?



#### A couple control strategies:

- 1. Average Controllability: Steer to many easily reachable states
- 2. **Modal Controllability:** Steer to few difficult to reach states

### Average and modal control

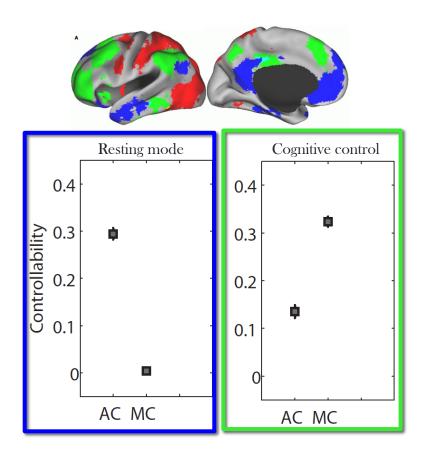


$$x(t+1) = Ax(t) + B_{\mathcal{K}}u_{\mathcal{K}}(t)$$
$$W_{\mathcal{K},T} = \sum_{\tau=0}^{T-1} A^{\tau} B_{\mathcal{K}} B_{\mathcal{K}}^{\mathsf{T}} (A^{\mathsf{T}})^{\tau}$$

**Average:** Trace(W<sub>K</sub><sup>-1</sup>))

**Modal**: Let  $v_j$  be the  $j^{th}$  eigenvector of A with eigenvalue  $\lambda_j$ . Then if  $v_{ij}$  is small, then the  $j^{th}$  mode is poorly controllable from node i. Define  $\phi_i = \sum_{j=1}^N (1 - \lambda_j^2(A)) v_{ij}^2$  as a scaled measure of controllability of all N modes from region i.)

### Controllability profiles differ across brain regions



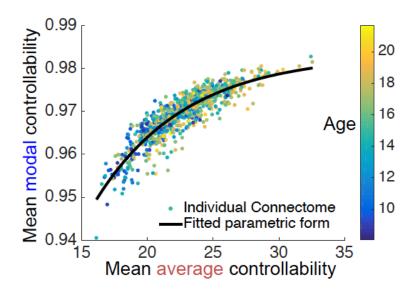
AC = average controllability MC = modal controllability Regions known to affect transient control of cognition are high in modal controllability, and are therefore structurally predisposed to push the brain to difficult-to-reach states.

Regions active at rest show white matter connectivity patterns predicted to effectively drive the brain to nearby brain states.



## Network control as a mechanism to effect cognition

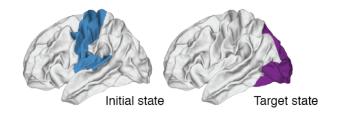
- Different brain regions have more or less power to alter whole-brain dynamics (Gu et al. 2015 Nature Communications)
- The capacity for brain regions to change brain dynamics grows as children develop (Tang et al. 2017 Nature Communications)
- Youth with greater network control also score better on cognitive tasks (Comblath et al. 2018 NeuroImage)

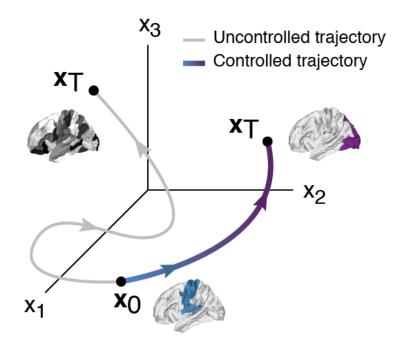


Together, these results suggest that our theory is a useful marker of how the brain enacts control to change network function.



## Precise control of specific state transitions





#### What we want

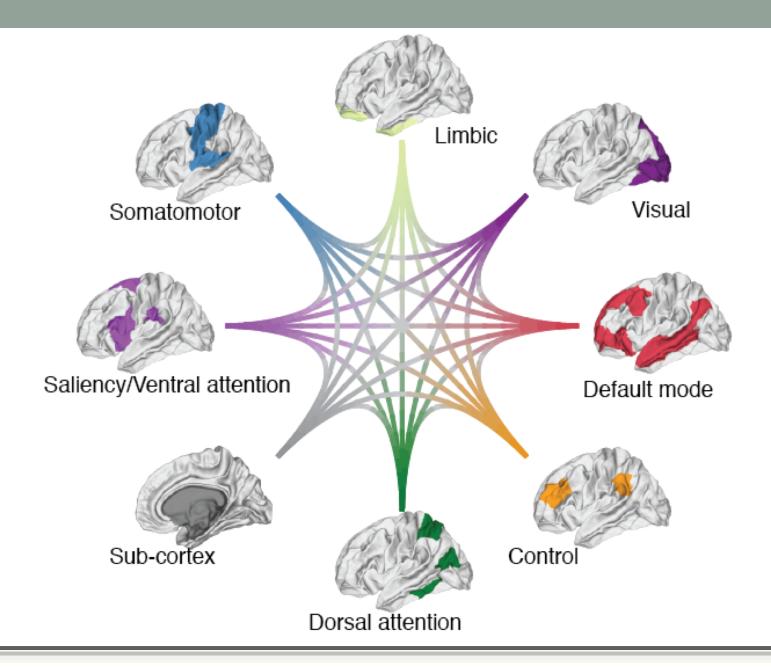
- Finite time, Finite energy,
  - Multi-point control
- Initial state, Target state

Define model of network dynamics.

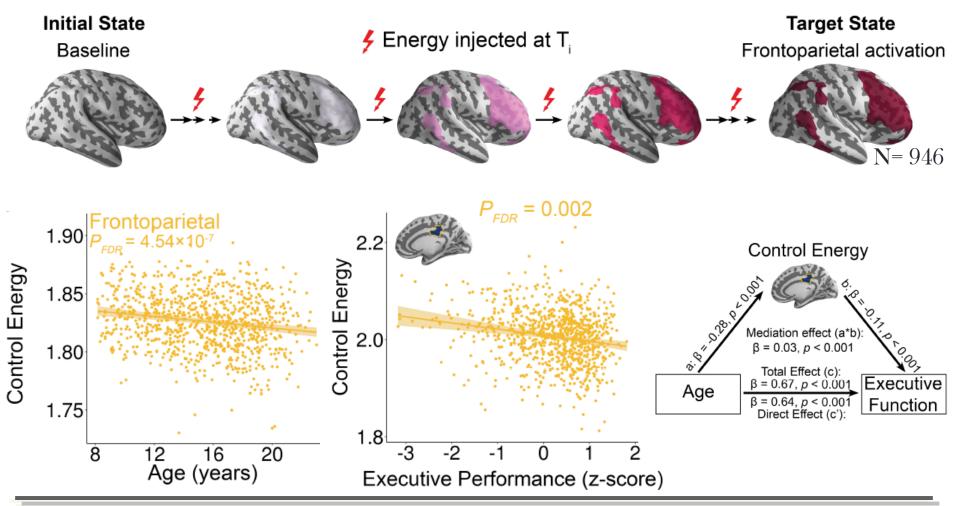
$$x(t+1) = Ax(t) + B_{\mathcal{K}}u_{\mathcal{K}}(t)$$

Define a cost function penalizes energy and distance of x(t) from the target state.

$$\min_{\mathbf{u}} \int_{0}^{T} (\mathbf{x}_{T} - \mathbf{x})^{T} (\mathbf{x}_{T} - \mathbf{x}) + \rho \mathbf{u}_{\mathcal{K}}^{T} \mathbf{u}_{\mathcal{K}}$$



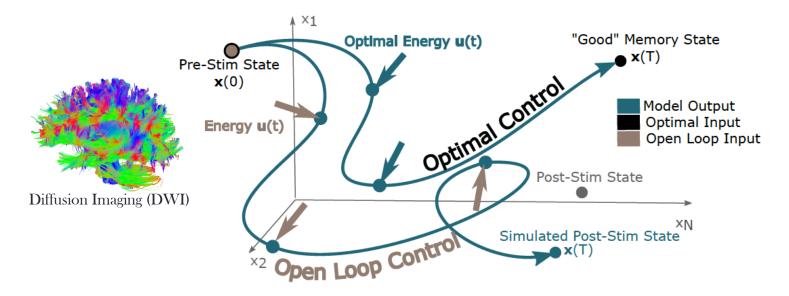
### Probing recruitment of the executive system



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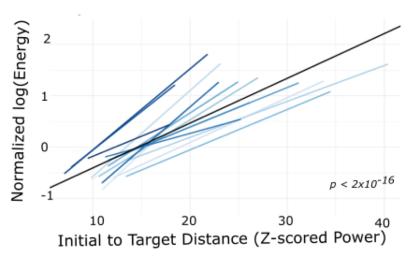
## Extending to exogenous control signals

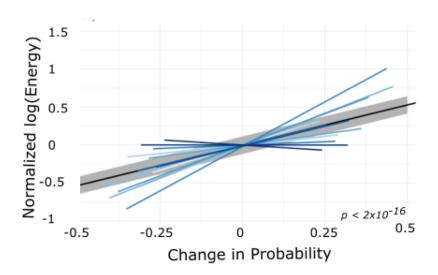
How does white matter network architecture guide direct electrical stimulation through optimal state transitions?



### Energy requirement depends on extent of transition

When enacting an optimal control transition from an initial state to a good memory state, the required energy depends on the distance in state space to be traversed ...





... and on the differences in cognitive state.

In fact, we can predict with 93.2% accuracy the energy required for a state transition using (i) transition distance, (ii) network topology, (iii) stimulation target.

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### VI. Summary: Network Neuroscience for Psychiatry

#### Where we are and where we could go

- Network science is one approach to address the complexity of neurobiological underpinnings of cognition, and its alteration in psychiatric conditions.
- The approach is flexible across data types, and provides statistics that can help us to quantitatively characterize networks representing neural circuits, behavioral transitions, and symptoms.
- It is fundamentally a modeling endeavor, with explicit assumptions. Care must be taken in choosing systems and scientific questions for which those assumptions are not violated.
- When engaging in the modeling endeavor, it behooves us to think carefully about model validation.
- Network control theory offers an option that could push us closer to predictive validity.



### Acknowledgments











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**Evelyn Tang** 



Shi Gu



John Medaglia



Ralf Schmaezle



Chad Giusti



Lizz Karuza











Rick Betzel



David Lydon-Staley



Marcelo Mattar



